



Model Building for Optimisation and Efficiency

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- Can I get a copy of the slides? Yes, we'll email links to download materials after the session has ended.
- Can we arrange a re-run for colleagues? Yes, just ask us.
- How can I ask questions? All lines are muted so please use the chat panel if we run out of time we will follow up with you.





A bit about SmartVision

We are vendor agnostic

We do Statistics/Data Science/Machine Learning/Optimisation/AI

We have some strategic partnerships ...



Our expertise spans commercial platforms and open source

We work across all sectors, all industries and many geographies

Our people have a long history in the domain

More about our offerings at the end of this presentation

Agenda

- What is optimisation, and what types of optimisation can be done?
- Example demonstrations
- Accessing optimisations easily



Prediction





Optimisation











SA

Types of Optimisation

			Model Type	Example
Туре	Example		linear	y = mx + c
	Matching a single value		Lineur	y = Aa + Bb + C
Single- objective	or Cost (minimising) or		New Baser	$y = ab + (ab)^2$
			Non-linear	Neural network
	Profit (maximising)			
	Matching multiple values			
Multi-	or Cost + Time (minimising) or		Model Type	Example
objective			Linear	y + z = Aa + Bb + C
	Protit (maximising) + People (minimising)		Non-linear	$Cost + Time = \frac{d^2y}{dt^2}x^2$



Increasing Complexity

I'd like to find the right balance between cost and time for my sorting process.

Conflicting Objectives

more people = less time = more cost

or less people = less cost = more time

Fast conclusion, or cheapest outcome?

Constraints

I can't employ more than x people

Project must be ready in y days

Overall cost can't surpass £z

I can employ more people, but they must cost less per person



Required Staff

	Monday	Tuesday	Wednesday	Thursday	Friday	Saturday	Sunday
Morning	9	12	8	10	13	10	14
Afternoon	11	13	10	11	9	11	7
Night	Night 8 7		5	15	7	8	6
Day	2	4	18	7	10	5	17

- Each shift requires different minimum resourcing, depending on the day
- Each staff member must work a minimum of 36 hours per week, and they cannot work on more than 5 days per week



- No one can work the Night shift immediately followed by a Morning shift
- Staff requirements (vacation leave etc.)
 - Emily Johnston can't work the Night shift on Monday
 - Emily Johnston can't work the Morning shift on Thursday
 - Don Harper can't work the Day shift on Tuesday
 - Mario Ryan can't work the Day shift on Wednesday
- Staff preferences
 - Don Harper prefers Morning and Day shifts
 - Chris Campbell prefers Afternoon shifts



- Not a trivial problem imagine doing this kind of rostering optimisation every week
- Use of specialised algorithms would help speed things up immensely
 - enter all the rules, such as those specified above
 - click Run
 - get results back in seconds, although they may not always be successful results, depending on the rules that are specified



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Afternoon	oon 11	13	10	11	9	11	7
Night	8	7	5	15	7	8	6
Day	2	4	18	7	10	5	17

Rostered Staff

	М	onda	у	Tuesday	Wednesday	Thursday	Friday	Saturday	Sunday
Morning	ning 9			12	8	10	13	10	14
Afternoon	on 11			13	10	11	9	11	7
Night	8			7	5	15	7	8	6
Day		5		4	18	7	10	5	17

 Each staff member must work a minimum of 36 hour per week, and they cannot work on more than 5 days per week







Emily Johnston	38	Timothy Chapman	36
Don Harper	38	Simon Harris	38
Mark Hawkins	38	Andy Farrell	40
Martha Ellis	38	Doug Douglas	36
Ben Campbell	40	Alexandra Dougla	38
Stephanie Richards	38	Jane Cole	36
John Evans	36	Vicoria Mysers	36
Sarah Brooks	36	Louise Owens	40
Alan Montgomery	38	Heath Robinson	36
Charles Hunt	36	Sarah Spencer	38
Victoria Owens	38	Vincent Brooks	36
Alex Brown	38	Harriet Turner	38
Richard Armstrong	36	Emily Elliott	40
Mark Murray	36	Adam Adams	38
Bob Evans	38	Mark Higgins	40
Melanie Brown	36	Joe Cole	40
Sam Thompson	40	Mario Ryan	38
Alex Ryan	36	Luke Wilson	38
Robert Carter	38	Julian Higgins	36
Joan Payne	36	Valerie Ryan	38
Sue Perkins	38	Charlene Perry	36
Tom West	38	Cameron Wright	40
Danielle Stevens	36	Fiona Myers	36
Liam Gibson	36	Charles Allen	36
Mark Crawford	36	Charlotte Stevens	38
Alex Barnes	38	Chris Campbell	40
Michael Howard	36	Harriet Myers	40

Staff Hours



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What if Chris Campbell doesn't mind working other shifts now?

Wednesday Thursday Monday Tuesday Friday Saturday Sunday Morning Afternoon Night Day

Rostered Staff

Required Staff

Morning 9 12 8 10 13 10 Afternoon 11 13 10 11 9 11	14
Afternoon 11 13 10 11 9 11	
	7
Night 8 7 5 15 7 8	6
Day 5 4 18 7 10 5	17

Old Rules

Rostered Staff

	Monday	Tuesday	Wednesday	Thursday	Friday	Saturday	Sunday
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Day	Day 4		18	7	10	6	17

New Rules











Staff Hours

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	Emily Johnston Don Harper Mark Hawkins Martha Ellis Ben Campbell Stephanie Richards John Evans Sarah Brooks Alan Montgomery Charles Hunt Victoria Owens Alex Brown Richard Armstrong Mark Murray Bob Evans Alex Brown Sam Thompson Alex Ryan Sam Thompson Alex Ryan Sue Perkins Joan Payne Sue Perkins Tom West Danielle Stevens Liam Gibson Mark Crawford Alex Barnes Michael Howard	Emily Johnston38Don Harper36Mark Hawkins36Martha Ellis36Ben Campbell36Stephanie Richards36John Evans40Sarah Brooks38Alan Montgomery36Charles Hunt38Victoria Owens38Alex Brown36Richard Armstrong40Mark Murray36Sam Thompson36Alex Ryan38Robert Carter36Joan Payne38Sue Perkins40Tom West36Liam Gibson36Mark Crawford40Alex Barnes36Michael Howard36	Emily Johnston38Timothy ChapmanDon Harper36Simon HarrisMark Hawkins36Andy FarrellMartha Ellis36Doug DouglasBen Campbell36Alexandra DouglaStephanie Richards36Jane ColeJohn Evans40Vicoria MysersSarah Brooks38Louise OwensAlan Montgomery36Heath RobinsonCharles Hunt38Sarah SpencerVictoria Owens38Vincent BrooksAlex Brown36Harriet TurnerRichard Armstrong40Emily ElliottMark Murray36Adam AdamsBob Evans36Mario RyanAlex Ryan38Luke WilsonRobert Carter36Jolian HigginsJoan Payne38Valerie RyanSue Perkins40Charlene PerryTom West36Fiona MyersLiam Gibson36Charlotte StevensAlex Barnes36Chris CampbellMichael Howard36Harriet Myers			



- Imagine extending this to hundreds of employees, with multiple rules related to different people – it would be pretty much impossible to do manually
- All of this rostering optimisation was done in Python using a specialised package called pyworkforce there other solutions out there that we could leverage too e.g. from AWS
- It could even be set up through a custom interface, where all the rules are entered simply, and every staff member gets an email with their weekly roster automatically

• This approach can also be extended to scheduling of services too



$$Loss = \sum_{i=1}^{n} \begin{cases} Constraint \ i \ met = 0 \\ Constraint \ i \ not \ met = 1 \end{cases}$$



- Imagine you work in a manufacturing environment, and you need to formulate a product by combining a number of ingredients
- But it gets interesting... you need to combine three ingredients, one each from three groups of ingredients, each with their own associated price, time to process and stock constraint, and the blend has to have a combined weight of 225 +/- 1 kg
- How would you go about optimising the perfect blend?



Group	Ingredient	Price (£/kg)	Time (min/kg)		Stock (kg)	
1	А	1.23	0.45	No obvious choic		
1	В	0.75	5 1.81		E - low price high time	
	С	2.26	0.62	C = hi	igh price, low ti	ime
2	D	5.21	1.54		102	
	E	0.34	1.55		123	
	F	3.33	1.23		155	
3	G	4.20	0.95		110	
	Н	5.99	0.66		107	



The problem means making the following decisions:

1. balancing price and time

What we are minimising – the optimisation

2. making sure that the batch size is correct

A constraint

3. ensuring that only one ingredient from each ingredient group is used in any batch

Think of it as having 16 variables \rightarrow

- each ingredient is being used or not (1 or 0) = 8 variables
- the quantity of each ingredient used in the optimisation = 8 variables

With 3 more constraints

- sum of A+B being used = 1
- sum of C+D+E being used = 1
- sum of F+G+H being used = 1



- There obviously are a vast number of possible combinations this problem could take remember it's not only time and price, but also which ingredient is used from each of three groups, and the total batch size must be 225 kg
- We therefore need to run an optimisation, minimising the time and price, while keeping within the constraints → we need a loss function

The lower the price and time, the smaller the loss (or "cost" to us)

A loss function is a calculation that calculates how much the formulation will "cost" us

$$Loss = (Price * Price_{weight}) + (Time * Time_{weight})$$

We can bias the loss towards Price
or Time by setting a weighting



- We ran this optimisation using a Bayesian Optimisation approach, as follows:
 - 10 initial random points, within the specific constraints
 - Ran the optimisation for a further 140 points
 - Each optimisation step evaluates 500 different samples, and selects the next one based on which of the samples will fill in the 16-dimensional variable space best
 - At the end of the optimisation, we selected the best 20 options out of the total of 150 points
- Why this approach...?



Convergence plot Starting cost: 260290 100000 Minimum cost: 38347 Minimum f(x) after n calls 90000 The "cost" is going down 80000 as more optimisation iterations are carried 70000 out, but not always Main improvement area Minor improvements (this means that the cost at 60000 each of the iterations is higher) 50000 40000 20 80 120 40 60 100 140 0 Number of calls n



- What if we had to make 3 consecutive batches, all with the same constraints and same ingredients... this is now a 48 (16 * 3) variable problem!
- With added complexity that individual ingredient stocks are limited!
- The optimisation would either simply take too long to be feasible, or else it would fail as there are too many constraints.
- For this we took more of a brute force approach, where we generated thousands of different samples this means that we leave finding the best options down to mere chance so, statistically, the more samples we run the more likely we are to find the best options



500 Iterations (Cost = 790473)						50,0	00 Iterat	ions (Co	st = 724	460)
h	ngredient	1	2	3	Stock	Ingredient	1	2	3	Stock
	А	164.9			164.9 (175)	А		170.7		170.7 (175)
	В		125.7	62.0	187.7 (200)	В	122.4		71.4	193.8 (200)
	С	56.6	33.6		90.2 (105)	С	55.1	47.8		102.9 (105)
	D				0 (102)	D				0 (102)
	Е			92.3	92.3 (123)	E			121.2	121.2 (123)
	F		65.7	70.8	136.5 (155)	F				0 (155)
	G				0 (110)	G	47.4	6.5	32.5	86.4 (110)
	н	3.5			3.5 (107)	н				0 (107)
	Sum	225	225	225		Sum	225	225	225	





Comparing Approaches

150 iterations in both cases

Bayesian Optimisation







A selection of Use Cases

Manufacturing & Operations

- Process Optimization: Tuning parameters for performance/safety
- Product formulation: Optimization: Balancing efficacy and cost
- Quality Control: Minimizing defects via optimal settings
- Resource Allocation: Assigning machines, labor, and materials efficiently





Supply Chain & Logistics

- Transportation Planning & Routing: Cost-effective shipping routes
- Inventory Optimization: Balancing holding costs vs. stock-outs
- Production Scheduling: Minimizing setup times and cost

Healthcare & Medical Applications

- Radiation Therapy Planning: Maximizing tumor targeting, minimizing harm
- Staff Scheduling: Meeting demand with workforce constraints
- Hospital Resource Allocation: OR schedules, bed capacities, supplies



A selection of Use Cases

Public Policy & Government Planning

- **Disaster Response & Evacuation**: Minimizing evacuation times/costs
- Urban Development & Zoning: Balancing economic
- and environmental goals
- **Resource Distribution**: Equitable allocation of public goods





Pharmaceutical & Biotechnology

- Drug Formulation Optimization: Balancing efficacy and cost
- Clinical Trial Optimization: Designing cost-effective, robust studies
- Pharma Supply Chain: Managing temperature-sensitive distribution

Transportation & Mobility Services

- Airline Scheduling & Crew Pairing: Reducing operational costs
- Ride-Sharing & Fleet Management: Real-time driver/passenger matching
- Urban Traffic Flow Optimization: Managing congestion via signal timing



Call center realtime scheduling

Assign incoming calls to agents based on required skills and minimize the customer waiting time.



Agent

Incoming calls





The AIMMS "Network Designer" is a map-based UI that lets us construct our supply chain network visually and optimize connections and flows based on that topography

Source: https://www.aimms.com/stories/extended-demo-aimms-network-design/

Smart Vision Service/Product Offerings

• CONSULTING SERVICES

Providing expert guidance and strategic advice to help organizations achieve their analytical goals

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